

Solving Quadratic Equations by Factoring

If a quadratic expression can be factored, then it is quite simple to solve by using the factors and the fact that if $a \cdot b = 0$ then either $a = 0$ or $b = 0$.

Examples:

$$\begin{aligned}x^2 - 5x + 6 &= 0 \\(x - 2)(x - 3) &= 0 \\x - 2 = 0 &\quad \text{or} \quad x - 3 = 0 \\x = 2 &\quad \text{or} \quad x = 3 \\&\text{two solutions}\end{aligned}$$

$$\begin{aligned}x^2 - 2x + 1 &= 0 \\(x - 1)(x - 1) &= 0 \\x - 1 = 0 &\quad \text{or} \quad x - 1 = 0 \\x = 1 &\quad \text{or} \quad x = 1 \\&\text{one solution}\end{aligned}$$

$$\begin{aligned}x^2 &= 36 \\x^2 - 36 &= 0 \\(x - 6)(x + 6) &= 0 \\x - 6 = 0 &\quad \text{or} \quad x + 6 = 0 \\x = 6 &\quad \text{or} \quad x = -6 \\&\text{two solutions}\end{aligned}$$

$$\begin{aligned}6x^2 + 5x &= 4 \\6x^2 + 5x - 4 &= 0 \\(2x - 1)(3x + 4) &= 0 \\2x - 1 = 0 &\quad \text{or} \quad 3x + 4 = 0 \\2x = 1 &\quad \text{or} \quad 3x = -4 \\x = \frac{1}{2} &\quad \text{or} \quad x = -\frac{4}{3}\end{aligned}$$