

### Factoring the sum or difference of cubes

If a polynomial is made up of the sum or difference of two perfect cubes, we have special rules to handle the factoring (these are not easy to memorize, I can never remember them without looking).

$$\begin{aligned} \mathbf{a^3 + b^3} &= \mathbf{(a + b)(a^2 - ab + b^2)} \\ \mathbf{a^3 - b^3} &= \mathbf{(a - b)(a^2 + ab + b^2)} \end{aligned}$$

Example:

$$\begin{aligned} \text{Factor } x^3 + 8 & \quad \text{note: } 8 = 2^3 \\ \text{Therefore, we get} & \\ x^3 + 2^3 & \quad a = x \text{ and } b = 2 \\ (x + 2)(x^2 - 2x + 2^2) & \\ (x + 2)(x^2 - 2x + 4) & \end{aligned}$$

Example:

$$\begin{aligned} \text{Factor } 64u^3 - 27v^6 & \quad \text{note: } 64u^3 = (4u)^3 \text{ and } 27v^6 = (3v^2)^3 \\ (4u)^3 - (3v^2)^3 & \quad a = 4u \text{ and } b = 3v^2 \\ (4u - 3v^2)((4u)^2 + (4u)(3v^2) + (3v^2)^2) & \\ (4u - 3v^2)(16u^2 + 12uv^2 + 3v^4) & \end{aligned}$$